# PART B:

# STATISTICS COMPLEMENTARY ELECTIVE COURSES

# [FOR B.Sc. MATHEMATICS / COMPUTER SCIENCE PROGRAMMES]

# WORK AND CREDIT DISTRIBUTION

# (2019 ADMISSION ONWARDS)

COURSE	COURSE TITLE	E TITLE SEMESTER	HOURS PER CREDIT	EXAM		MARKS		
CODE	COURSE IIILE	SEVIESTER	WEEK	CREDIT	HOURS	CE	ESE	TOTAL
1C01 STA	BASIC STATISTICS	Ι	4	3	3	10	40	50
2C02 STA	PROBABILITY THEORY AND RANDOM VARIABLES	п	4	3	3	10	40	50
3C03 STA	PROBABILITY DISTRIBUTIONS	III	5	3	3	10	40	50
4C04 STA	STATISTICAL INFERENCE	IV	5	3	3	10	40	50

# **EVALUATION**

ASSESSMENT	WEIGHTAGE
EXTERNAL	4
INTERNAL	1

# **INTERNAL ASSESSMENT**

COMPONENT	WEIGHTAGE	REMARKS
COMPONENT 1 TEST PAPER	3	For each theory course there shall be a minimum of 3 written tests and the average mark of the best two tests is to be considered for internal mark. Each test paper may have duration of minimum one hour.
<b>COMPONENT 2</b> ASSIGNMENT/ SEMINAR/VIVA	1	For each theory course each student is required to submit two assignments or to present a seminar or to attend a viva- voce. Assignments /seminar / viva-voce shall be evaluated on the basis of student performance.

#### COMPLEMENTARY ELECTIVE COURSE I: BASIC STATISTICS

SEMESTER	COURSE CODE	HOURS PER WEEK	CREDIT	EXAM HRS
I	1C01 STA	4	3	3

# **COURSE OUTCOME**

Student should be able to

**CO1:** understand the different types of data.

CO2: compute various measures of central tendency, measures of variation.

**CO3:** analyse the relationship between two variables.

CO4: acquire knowledge in time series data and compute various index numbers.

**Unit I : Statistical Methods -** Scales of measurement - Nominal, Ordinal, Ratio and Interval, Collection of data, Primary and Secondary data, Census method, Sample survey method, Comparison of census method and sample survey method, Principal steps in a sample survey, Types of sampling - probability, restricted and non-restricted sampling, judgement and mixed sampling, SRSWOR, SRSWR, stratified and systematic random sampling(concepts only).

#### (12 Hrs.)

**Unit II : Measures of Central Tendency** Definition and properties of various measures of central tendency - A.M,weighted A.M, Median, Mode, G.M., H.M. and weighted averages, Partition values - Quartiles, Deciles, Percentiles, Dispersion - Definition and properties of various measures of dispersion - Range, Q.D, M.D, S.D, and relative measures of dispersion, Moments - raw moments, central moments and relation between them, Skewness and Kurtosis - Definition and various measures of skewness and kurtosis.

# (30 Hrs)

**Unit III: Correlation and Regression Analysis** - Method of least squares - Fitting of linear, quadratic and exponential curves, Regression analysis - linear regression, fitting of regression lines, regression coefficients and their properties, Correlation analysis - Definition and properties of correlation coefficient, Rank correlation coefficient-formula and problems only, Definitions of partial and multiple correlation coefficients(trivariate case only).

# (18 Hrs)

Unit IV: Time Series and Index Numbers- Time series - Meaning, need, components and models of time series, estimation of linear trend by moving average

method and least square method, Index numbers - Meaning and uses of index numbers, weighted index numbers - Laspeyer's, Paasche's and Fisher's index numbers, time reversal and factor reversal tests.

#### (12 Hrs)

#### **Books for Study:**

- 1. Gupta, S. C. & Kapoor, V. K. (1980). *Fundamentals of Mathematical Statistics*, Sultan Chand & Sons, New Delhi.
- 2. Gupta, S. C. & Kapoor, V. K. (1994). *Fundamentals of Applied Statistics*, Sultan Chand & Sons, New Delhi.
- 3. Gupta, S. P. (2004). Statistical Methods, Sultan Chand & Sons, New-Delhi.

#### **Books for Reference:**

- 1. Mukhopadhyay, P. (1996). *Mathematical Statistics*, New Central Book Agency (P) Ltd., Kolkata.
- **2.** Agarwal, B. L. (2006). *Basic Statistics*, 4<sup>th</sup> Edition, New Age International (P) Ltd., New Delhi.

#### Marks including choice:

Unit	Unit I	Unit II	Unit III	Unit IV	Total
Marks	10	20	15	15	60

Part A -	Short answer	(6 questions x Mark $1 = 6$ )
	• Answer all questions	(6 questions x Mark $1 = 6$ )
Part B -	Short Essay	(8 questions x Marks 2 each =16)
	• Answer any 6questions	(6questions x Marks 2 each=12)
Part C -	Essay	(6 questions x Marks 3 each =18)
	• Answer any 4 questions	( 4 questions x Marks 3 each=12)
Part D -	Long Essay	(4 questions x Marks 5 each =20)
	• Answer any 2 questions	( 2 questions x Marks 5 each=10)

- Total marks including choice -60
- Maximum marks of the course- 40

# COMPLEMENTARY ELECTIVE COURSE II: PROBABILITY THEORY AND RANDOM VARIABLES

SEMESTER	COURSE CODE	HOURS PER WEEK	CREDIT	EXAM HRS
II	2C02STA	4	3	3

#### **COURSE OUTCOME**

Student should be able to

**CO 1:** evaluate the probability of events.

- CO 2: understand the concept of random variables with examples in real life
- **CO3:** calculate the probability distribution of discrete and continuous random variables.
- **CO 4:** understand the change of variable technique.

#### **Unit I: Probability Theory-I**

Random experiments, sample space, events, classical definition and frequency approach to probability, laws of events, sigma field, axiomatic definition of probability, probability space, addition theorem (2 and 3 events), Boole's inequalities.

(25 Hrs)

#### **Unit II: Probability Theory-II**

Conditional probability, multiplication theorem, independence of events, pair wise and mutual independence, Baye's theorem and its applications.

# (18 Hrs)

**Unit III: Random Variables** - Discrete and continuous random variables, probability mass function and probability density function, distribution function - definition and properties, transformation of random variables-discrete and continuous.

#### (17 Hrs)

**Unit IV: Bivariate Random Variables** - Definitions, joint probability distributions, marginal and conditional distributions, independence of random variables, transformations of bivariate random variables.

#### (12 Hrs)

#### **Books for Study:**

1. Gupta, S. C. &Kapoor, V. K. (1980). *Fundamentals of Mathematical Statistics*, Sultan Chand & Sons, New Delhi.

#### **Books for Reference:**

1. Rao, C. R. (1973). Linear Statistical Inference and its Applications, 2/e, Wiley, New York.

- 2. Dudewicz, E. J. & Mishra S. N. (1988). Modern Mathematical Statistics, John Wiley & Sons, New York.
- 3. Pitman, J. (1993). Probability, Narosa Publishing House, New Delhi.
- 4. Rohatgi, V. K. (1993). An Introduction to Probability Theory and Mathematical Statistics, Wiley Eastern, New Delhi. Hsu, H. P. (1997).
- 5. Hsu,H.P.(1997) Schaum's Outline of Theory and Problems of Probability, Random Variables and Random Processes, The McGraw-Hill Companies, Inc., New York.
- 6. Lipschutz, S.& Schiller, J. J. (1998). Schaum's Outline of Theory and Problems of Introduction to Probability and Statistics, The McGraw-Hill Companies, Inc., New York.

Marks including choice:

Unit	Unit I	Unit II	Unit III	Unit IV	Total
Marks	20	15	15	10	60

Part A -	Short answer	(6 questions x Mark $1 = 6$ )
	Answer all questions	(6 questions x Mark $1 = 6$ )
Part B -	Short Essay	(8 questions x Marks 2 each =16)
	• Answer any 6questions	(6questions x Marks 2 each=12)
Part C -	Essay	(6 questions x Marks 3 each =18)
	• Answer any 4 questions	( 4 questions x Marks 3 each=12)
Part D -	Long Essay	(4 questions x Marks 5 each =20)
	• Answer any 2 questions	(2 questions x Marks 5 each=10)

- Total marks including choice -60
- Maximum marks of the course- 40

# COMPLEMENTARY ELECTIVE COURSE III: PROBABILITY DISTRIBUTIONS

SEMESTER	COURSE CODE	HOURS PER WEEK	SEMESTER	COURSE CODE
III	3C03 STA	5	3	3

# **COURSE OUTCOME**

Student should be able to

**CO1:** compute mathematical expectation of a random variable.

- **CO2:** familiarize with different discrete probability distribution associated with real life situations.
- CO3: understand the characteristics of different continuous distributions.

CO4: identify the appropriate probability model that can be used.

**Unit I: Mathematical Expectation:** Definition and properties of mathematical expectation, Addition and multiplication theorem on expectation, Expectation of functions of random variables, Moments - Definition of raw and central moments, relation between raw and central moments, Expectation of bivariate random variables, conditional mean and variance, Coefficient of correlation between random variables. Moment generating function - Definition and properties, Characteristic function - Definition and properties.

#### (22 Hrs)

**Unit II: Discrete Distributions -** Definition, moments, m.g.f., characteristic function, properties and different characteristics of discrete uniform distribution, Bernoulli distribution, Binomial distribution, Poisson distribution and Geometric distribution.

(25 Hrs)

**Unit III: Continuous Distributions** Definition, moments, m.g.f., characteristic function, properties and different characteristics of Uniform distribution, Normal distribution, Standard normal distribution, Exponential distribution, Gamma distribution with one and two parameters, Beta distributions of I and II kind.

# (25 Hrs)

**Unit IV: Sampling distributions -** Definition, standard error, sampling distribution of sample mean and sample variance, Chi-square, Student's t and F distributions, Interrelations between chi-square, t and F distributions.

(18Hrs)

#### **Books for Study:**

- 1. Gupta, S. C. &Kapoor, V. K. (1980). Fundamentals of Mathematical Statistics, Sultan Chand & Sons, New Delhi.
- 2. Goon, A. M., Gupta, M. K. & Dasgupta, B. (2003). *An Outline of Statistical Theory*, Volume I, 4<sup>th</sup>Edn, The World Press Pvt. Ltd., Kolkata.

# **Books for Reference:**

- 1. John E. Freund (1980). *Mathematical Statistics*, Prentice Hall of India, New Delhi.
- 2. Rohatgi, V. K. (1993). An Introduction to Probability Theory and Mathematical Statistics, Wiley Eastern, New Delhi.
- Mood, A. M., Graybill, F. A. &Boes, D. C. (2007). *Introduction to the Theory* of Statistics, 3<sup>rd</sup>Edn (Reprint). Tata McGraw-Hill Publishing Company Ltd., New Delhi.

#### Marks including choice:

Unit	Unit I	Unit II	Unit III	Unit IV	Total
Marks	14	17	17	12	60

Part A -	Short answer	(6 questions x Mark $1 = 6$ )
	• Answer all questions	(6 questions x Mark $1 = 6$ )
Part B -	Short Essay	(8 questions x Marks 2 each =16)
	• Answer any 6questions	(6questions x Marks 2 each=12)
Part C -	Essay	(6 questions x Marks 3 each =18)
	• Answer any 4 questions	( 4 questions x Marks 3 each=12)
Part D -	Long Essay	(4 questions x Marks 5 each =20)
	• Answer any 2 questions	( 2 questions x Marks 5 each=10)

- Total marks including choice -60
- Maximum marks of the course- 40

# COMPLEMENTARY ELECTIVE COURSE IV: STATISTICAL INFERENCE

SEMESTER	COURSE CODE	HOURS PER WEEK	CREDIT	EXAM HRS
IV	4C04 STA	5	3	3

# **COURSE OUTCOME**

Student should be able to

CO 1: understand the uses of Chebychev's Inequality and Central Limit Theorem.

CO 2: apply various method of estimation

**CO 3:** understand the concept of testing statistical hypotheses and its importance in real life situation

CO 4: apply ANOVA

**Unit I: Chebychev's Inequality and Law of Large Numbers** Chebychev's Inequality and its applications, convergence in probability, Weak law of large numbers, Bernoulli's law of large numbers, Convergence in distribution and central limit theorem for IID random variables (Statement only).

# (15 Hrs)

**Unit II: Theory of Estimation** Point estimation, Desirable properties of a good estimator, Cramer-Rao inequality (statement only), Methods of estimation - method of MLE and method of moments. Interval estimation - Confidence interval for mean, proportion, variance, difference of means, difference of proportions.

# (25 Hrs)

**Unit III : Testing of Hypotheses -** Statistical hypotheses, Simple and composite hypotheses, Null and alternative hypotheses, Types of errors, Critical region, Size and power of test – Definition and problems, most powerful test, Neyman - Pearson lemma (without proof).

# (20 Hrs)

**Unit IV: Large and small sample tests** - Test for mean, proportion, equality of means, equality of proportions, paired t-test, test for variance and equality of variance, Chi-square test for goodness of fit, test for independence of attributes, One-way ANOVA (assumptions and problem only).

# (30 Hrs)

<u>NOTE:</u> Numerical computations involved in Assignments submitted may preferably be done using any computer packages.

#### **Books for Study:**

- 1. Gupta, S. C. & Kapoor, V. K. (1980). *Fundamentals of Mathematical Statistics*, Sultan Chand & Sons, New Delhi.
- 2. Gupta, S. C. &Kapoor, V. K. (1994). *Fundamentals of Applied Statistics*, Sultan Chand & Sons, New Delhi.

#### **Books for Reference:**

- 1. John E. Freund (1980). *Mathematical Statistics*, Prentice Hall of India, New Delhi.
- **2.** Rohatgi, V. K. (1993). An Introduction to Probability Theory and Mathematical Statistics, Wiley Eastern, New Delhi.
- **3.** Medhi, J. (2005). *Statistical Methods-An Introductory Text*, New Age International (P) Ltd., New Delhi.
- **4.** Spiegel, M. R., Schiller, J. J. & Srinivasan, R. A. (2013). *Schaum's Outline of Probability and Statistics*, 4<sup>th</sup>Edn. The McGraw-Hill Companies, Inc., New York.

Marks including choice:

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Marks	10	17	13	20	60

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Part C -	Essay	(6 questions x Marks 3 each =18)
	• Answer any 4 questions	(4 questions x Marks 3 each=12)
Part D -	Long Essay	(4 questions x Marks 5 each =20)
	• Answer any 2 questions	(2 questions x Marks 5 each=10)

- Total marks including choice -60
- Maximum marks of the course- 40