## PART B:

## STATISTICS COMPLEMENTARY ELECTIVE COURSES

[FOR B.Sc. MATHEMATICS / COMPUTER SCIENCE PROGRAMMES]

## WORK AND CREDIT DISTRIBUTION

(2019 ADMISSION ONWARDS)

| COURSE CODE | COURSE TITLE | SEMESTER | HOURS <br> PER <br> WEEK | CREDIT | EXAM HOURS | MARKS |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | CE | ESE | TOTAL |
| $1 \mathrm{C01} \mathrm{STA}$ | BASIC STATISTICS | I | 4 | 3 | 3 | 10 | 40 | 50 |
| $2 \mathrm{C02}$ STA | PROBABILITY <br> THEORY AND <br> RANDOM <br> VARIABLES | II | 4 | 3 | 3 | 10 | 40 | 50 |
| 3C03 STA | PROBABILITY <br> DISTRIBUTIONS | III | 5 | 3 | 3 | 10 | 40 | 50 |
| 4C04 STA | STATISTICAL INFERENCE | IV | 5 | 3 | 3 | 10 | 40 | 50 |

## EVALUATION

| ASSESSMENT | WEIGHTAGE |
| :---: | :---: |
| EXTERNAL | 4 |
| INTERNAL | 1 |

## INTERNAL ASSESSMENT

| COMPONENT | WEIGHTAGE | REMARKS |
| :---: | :---: | :--- |
| COMPONENT 1 | $\mathbf{3}$ | For each theory course there shall be a <br> minimum of 3 written tests and the <br> average mark of the best two tests is to <br> be considered for internal mark. Each <br> test paper may have duration of <br> minimum one hour. |
| TEST PAPER | $\mathbf{1}$ | For each theory course each student is <br> required to submit two assignments or <br> to present a seminar or to attend a viva- <br> voce. Assignments /seminar / viva-voce <br> shall be evaluated on the basis of <br> student performance. |
| COMPONENT 2 |  |  |
| ASSIGNMENT/ |  |  |

COMPLEMENTARY ELECTIVE COURSE I: BASIC STATISTICS

| SEMESTER | COURSE CODE | HOURS <br> PER WEEK | CREDIT | EXAM <br> HRS |
| :---: | :---: | :---: | :---: | :---: |
| I | 1C01 STA | 4 | 3 | 3 |

## COURSE OUTCOME

Student should be able to
CO1: understand the different types of data.
CO2: compute various measures of central tendency, measures of variation.
CO3: analyse the relationship between two variables.
CO4: acquire knowledge in time series data and compute various index numbers.

Unit I : Statistical Methods - Scales of measurement - Nominal, Ordinal, Ratio and Interval, Collection of data, Primary and Secondary data, Census method, Sample survey method, Comparison of census method and sample survey method, Principal steps in a sample survey, Types of sampling - probability, restricted and non-restricted sampling, judgement and mixed sampling, SRSWOR, SRSWR, stratified and systematic random sampling(concepts only).
(12 Hrs.)
Unit II : Measures of Central Tendency Definition and properties of various measures of central tendency - A.M,weighted A.M, Median, Mode, G.M., H.M. and weighted averages, Partition values - Quartiles, Deciles, Percentiles, Dispersion Definition and properties of various measures of dispersion - Range, Q.D, M.D, S.D, and relative measures of dispersion, Moments - raw moments, central moments and relation between them, Skewness and Kurtosis - Definition and various measures of skewness and kurtosis.
(30 Hrs)
Unit III: Correlation and Regression Analysis - Method of least squares - Fitting of linear, quadratic and exponential curves, Regression analysis - linear regression, fitting of regression lines, regression coefficients and their properties, Correlation analysis - Definition and properties of correlation coefficient, Rank correlation coefficient-formula and problems only, Definitions of partial and multiple correlation coefficients(trivariate case only).
(18 Hrs)

Unit IV: Time Series and Index Numbers- Time series - Meaning, need, components and models of time series, estimation of linear trend by moving average
method and least square method, Index numbers - Meaning and uses of index numbers, weighted index numbers - Laspeyer's, Paasche's and Fisher's index numbers, time reversal and factor reversal tests.
(12 Hrs)

## Books for Study:

1. Gupta, S. C. \& Kapoor, V. K. (1980). Fundamentals of Mathematical Statistics, Sultan Chand \& Sons, New Delhi.
2. Gupta, S. C. \& Kapoor, V. K. (1994). Fundamentals of Applied Statistics, Sultan Chand \& Sons, New Delhi.
3. Gupta, S. P. (2004). Statistical Methods, Sultan Chand \& Sons, New-Delhi.

## Books for Reference:

1. Mukhopadhyay, P. (1996). Mathematical Statistics, New Central Book Agency (P) Ltd., Kolkata.
2. Agarwal, B. L. (2006). Basic Statistics, $4^{\text {th }}$ Edition, New Age International (P) Ltd., New Delhi.

## Marks including choice:

| Unit | Unit I | Unit II | Unit III | Unit IV | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Marks | 10 | 20 | 15 | 15 | 60 |

## About the Pattern of Questions:

| Part $A$ | Short answer | (6 questions x Mark $1=6$ ) |
| :---: | :---: | :---: |
|  | - Answer all questions | (6 questions $x$ Mark $1=6$ ) |
| Part B - | Short Essay | (8 questions x Marks 2 each = 16) |
|  | - Answer any 6questions | (6questions x Marks 2 each=12) |
| Part C- | Essay | (6 questions x Marks 3 each =18) |
|  | - Answer any 4 questions | ( 4 questions $x$ Marks 3 each=12) |
| Part D - | Long Essay | (4 questions x Marks 5 each =20) |
|  | - Answer any 2 questions | ( 2 questions $x$ Marks 5 each=10) |

- Total marks including choice -60
- Maximum marks of the course- 40

COMPLEMENTARY ELECTIVE COURSE II: PROBABILITY THEORY AND RANDOM VARIABLES

| SEMESTER | COURSE CODE | HOURS <br> PER WEEK | CREDIT | EXAM <br> HRS |
| :---: | :---: | :---: | :---: | :---: |
| II | 2C02STA | 4 | 3 | 3 |

## COURSE OUTCOME

Student should be able to
CO 1: evaluate the probability of events.
CO 2: understand the concept of random variables with examples in real life
CO3: calculate the probability distribution of discrete and continuous random variables.
CO 4: understand the change of variable technique.

## Unit I: Probability Theory-I

Random experiments, sample space, events, classical definition and frequency approach to probability, laws of events, sigma field, axiomatic definition of probability, probability space, addition theorem ( 2 and 3 events), Boole's inequalities.
( 25 Hrs )

## Unit II: Probability Theory-II

Conditional probability, multiplication theorem, independence of events, pair wise and mutual independence, Baye's theorem and its applications.
(18 Hrs)

Unit III: Random Variables - Discrete and continuous random variables, probability mass function and probability density function, distribution function - definition and properties, transformation of random variables-discrete and continuous.

Unit IV: Bivariate Random Variables - Definitions, joint probability distributions, marginal and conditional distributions, independence of random variables, transformations of bivariate random variables.
(12 Hrs)

## Books for Study:

1. Gupta, S. C. \&Kapoor, V. K. (1980). Fundamentals of Mathematical Statistics, Sultan Chand \& Sons, New Delhi.

## Books for Reference:

1. Rao, C. R. (1973). Linear Statistical Inference and its Applications, 2/e, Wiley, New York.
2. Dudewicz, E. J. \& Mishra S. N. (1988). Modern Mathematical Statistics, John Wiley \& Sons, New York.
3. Pitman, J. (1993). Probability, Narosa Publishing House, New Delhi.
4. Rohatgi, V. K. (1993). An Introduction to Probability Theory and Mathematical Statistics, Wiley Eastern, New Delhi. Hsu, H. P. (1997).
5. Hsu,H.P.(1997) Schaum's Outline of Theory and Problems of Probability, Random Variables and Random Processes, The McGraw-Hill Companies, Inc., New York.
6. Lipschutz, S.\& Schiller, J. J. (1998). Schaum's Outline of Theory and Problems of Introduction to Probability and Statistics, The McGraw-Hill Companies, Inc., New York.

## Marks including choice:

| Unit | Unit I | Unit II | Unit III | Unit IV | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Marks | 20 | 15 | 15 | 10 | 60 |

About the Pattern of Questions:

| Part A - | Short answer <br> - Answer all questions | $\begin{aligned} & (6 \text { questions x Mark } 1=6) \\ & (6 \text { questions } \times \text { Mark } 1=6) \end{aligned}$ |
| :---: | :---: | :---: |
| Part B - | Short Essay <br> - Answer any 6questions | $\begin{aligned} & (8 \text { questions x Marks } 2 \text { each }=16 \text { ) } \\ & \text { (6questions } x \text { Marks } 2 \text { each=12) } \end{aligned}$ |
| Part C- | Essay <br> - Answer any 4 questions | $\begin{aligned} & (6 \text { questions } x \text { Marks } 3 \text { each }=18 \text { ) } \\ & (4 \text { questions } x \text { Marks } 3 \text { each }=12 \text { ) } \end{aligned}$ |
| Part D - | Long Essay <br> - Answer any 2 questions | $\begin{aligned} & (4 \text { questions x Marks } 5 \text { each }=20 \text { ) } \\ & (2 \text { questions } x \text { Marks } 5 \text { each }=10 \text { ) } \end{aligned}$ |

- Total marks including choice -60
- Maximum marks of the course- 40


## COMPLEMENTARY ELECTIVE COURSE III: PROBABILITY DISTRIBUTIONS

| SEMESTER | COURSE CODE | HOURS <br> PER WEEK | SEMESTER | COURSE <br> CODE |
| :---: | :---: | :---: | :---: | :---: |
| III | 3C03 STA | 5 | 3 | 3 |

## COURSE OUTCOME

Student should be able to
CO1: compute mathematical expectation of a random variable.
CO2: familiarize with different discrete probability distribution associated with real life situations.
CO3: understand the characteristics of different continuous distributions.
CO4: identify the appropriate probability model that can be used.

Unit I: Mathematical Expectation: Definition and properties of mathematical expectation, Addition and multiplication theorem on expectation, Expectation of functions of random variables, Moments - Definition of raw and central moments, relation between raw and central moments, Expectation of bivariate random variables, conditional mean and variance, Coefficient of correlation between random variables. Moment generating function - Definition and properties, Characteristic function Definition and properties.
(22 Hrs)

Unit II: Discrete Distributions - Definition, moments, m.g.f., characteristic function, properties and different characteristics of discrete uniform distribution, Bernoulli distribution, Binomial distribution, Poisson distribution and Geometric distribution.
(25 Hrs)

Unit III: Continuous Distributions Definition, moments, m.g.f., characteristic function, properties and different characteristics of Uniform distribution, Normal distribution, Standard normal distribution, Exponential distribution, Gamma distribution with one and two parameters, Beta distributions of I and II kind.
(25 Hrs)
Unit IV: Sampling distributions - Definition, standard error, sampling distribution of sample mean and sample variance, Chi-square, Student's t and F distributions, Interrelations between chi-square, t and F distributions.

## Books for Study:

1. Gupta, S. C. \&Kapoor, V. K. (1980). Fundamentals of Mathematical Statistics, Sultan Chand \& Sons, New Delhi.
2. Goon, A. M., Gupta, M. K. \& Dasgupta, B. (2003). An Outline of Statistical Theory, Volume I, $4^{\text {th }}$ Edn, The World Press Pvt. Ltd., Kolkata.

## Books for Reference:

1. John E. Freund (1980). Mathematical Statistics, Prentice Hall of India, New Delhi.
2. Rohatgi, V. K. (1993). An Introduction to Probability Theory and Mathematical Statistics, Wiley Eastern, New Delhi.
3. Mood, A. M., Graybill, F. A. \&Boes, D. C. (2007). Introduction to the Theory of Statistics, $3{ }^{\text {rd }}$ Edn (Reprint). Tata McGraw-Hill Publishing Company Ltd., New Delhi

Marks including choice:

| Unit | Unit I | Unit II | Unit III | Unit IV | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Marks | 14 | 17 | 17 | 12 | 60 |

About the Pattern of Questions:

| Part A - | Short answer <br> - Answer all questions | $\begin{aligned} & (6 \text { questions x Mark } 1=6) \\ & (6 \text { questions } x \text { Mark } 1=6) \end{aligned}$ |
| :---: | :---: | :---: |
| Part B - | Short Essay <br> - Answer any 6questions | $\begin{aligned} & \text { (8 questions x Marks } 2 \text { each }=16 \text { ) } \\ & \text { (6questions } x \text { Marks } 2 \text { each=12) } \end{aligned}$ |
| Part C - | Essay <br> - Answer any 4 questions | $\begin{aligned} & (6 \text { questions x Marks } 3 \text { each }=18) \\ & (4 \text { questions } x \text { Marks } 3 \text { each }=12 \text { ) } \end{aligned}$ |
| Part D - | Long Essay <br> - Answer any 2 questions | (4 questions x Marks 5 each =20) <br> ( 2 questions $x$ Marks 5 each=10) |

- Total marks including choice -60
- Maximum marks of the course- 40

COMPLEMENTARY ELECTIVE COURSE IV: STATISTICAL INFERENCE

| SEMESTER | COURSE CODE | HOURS <br> PER WEEK | CREDIT | EXAM <br> HRS |
| :---: | :---: | :---: | :---: | :---: |
| IV | 4C04 STA | 5 | 3 | 3 |

COURSE OUTCOME
Student should be able to
CO 1: understand the uses of Chebychev's Inequality and Central Limit Theorem.
CO 2: apply various method of estimation
CO 3: understand the concept of testing statistical hypotheses and its importance in real life situation
CO 4: apply ANOVA
Unit I: Chebychev's Inequality and Law of Large Numbers Chebychev's Inequality and its applications, convergence in probability, Weak law of large numbers, Bernoulli's law of large numbers, Convergence in distribution and central limit theorem for IID random variables (Statement only).
(15 Hrs)
Unit II: Theory of Estimation Point estimation, Desirable properties of a good estimator, Cramer-Rao inequality (statement only), Methods of estimation - method of MLE and method of moments. Interval estimation - Confidence interval for mean, proportion, variance, difference of means, difference of proportions.
(25 Hrs)
Unit III : Testing of Hypotheses - Statistical hypotheses, Simple and composite hypotheses, Null and alternative hypotheses, Types of errors, Critical region, Size and power of test - Definition and problems, most powerful test, Neyman - Pearson lemma (without proof).
(20 Hrs)
Unit IV: Large and small sample tests - Test for mean, proportion, equality of means, equality of proportions, paired $t$-test, test for variance and equality of variance, Chi-square test for goodness of fit, test for independence of attributes, One-way ANOVA (assumptions and problem only).

NOTE: Numerical computations involved in Assignments submitted may preferably be done using any computer packages.

## Books for Study:

1. Gupta, S. C. \& Kapoor, V. K. (1980). Fundamentals of Mathematical Statistics, Sultan Chand \& Sons, New Delhi.
2. Gupta, S. C. \&Kapoor, V. K. (1994). Fundamentals of Applied Statistics, Sultan Chand \& Sons, New Delhi.

## Books for Reference:

1. John E. Freund (1980). Mathematical Statistics, Prentice Hall of India, New Delhi.
2. Rohatgi, V. K. (1993). An Introduction to Probability Theory and Mathematical Statistics, Wiley Eastern, New Delhi.
3. Medhi, J. (2005). Statistical Methods-An Introductory Text, New Age International (P) Ltd., New Delhi.
4. Spiegel, M. R., Schiller, J. J. \&Srinivasan, R. A. (2013). Schaum's Outline of Probability and Statistics, $4^{\text {th }}$ Edn. The McGraw-Hill Companies, Inc., New York.

Marks including choice:

| Unit | Unit I | Unit II | Unit III | Unit IV | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Marks | 10 | 17 | 13 | 20 | 60 |

About the Pattern of Questions:

| Part A - | Short answer <br> - Answer all questions | (6 questions x Mark $1=6$ ) <br> (6 questions x Mark $1=6$ ) |
| :---: | :---: | :---: |
| Part B - | Short Essay <br> - Answer any 6questions | $\begin{aligned} & \text { (8 questions x Marks } 2 \text { each }=16 \text { ) } \\ & \text { (6questions } x \text { Marks } 2 \text { each=12) } \end{aligned}$ |
| Part C - | Essay <br> - Answer any 4 questions | (6 questions x Marks 3 each $=18$ ) <br> ( 4 questions $x$ Marks 3 each=12) |
| Part D - | Long Essay <br> - Answer any 2 questions | (4 questions $x$ Marks 5 each =20) <br> ( 2 questions $x$ Marks 5 each=10) |

- Total marks including choice -60
- Maximum marks of the course- 40

