### DON BOSCO ARTS & SCIENCE COLLEGE ANGADIKADAVU

(Affiliated to Kannur University Approved by Government of Kerala) ANGADIKADAVU P.O., IRITTY, KANNUR – 670706



# **COURSE PLAN**

# **MSc Mathematics**

### (2021 - 23)

## **SEMESTER - III**

## **ACADEMIC YEAR - (2022-23)**

|            | III Semester MSc Matheatics (2021 - 23)                              |               |   |  |  |  |  |
|------------|--|---------------|---|--|--|--|--|
| SL.<br>No. | Name of Subjects with Code Name of the Teacher Duty Hours   per week |               |   |  |  |  |  |
| 1.         | MAT3C11 Number Theory  | Najumunnisa.K | 5 |  |  |  |  |
| 2.         | MAT3C12 Functional Analysis  | Anil M V      | 5 |  |  |  |  |
| 3.         | MAT3C13 Complex function theory                                      | Riya Baby     | 5 |  |  |  |  |
| 4.         | MAT3C14 Advanced Real Analysis                                       | Athulya P     | 5 |  |  |  |  |
| 5.         | MAT3E01: Elective Graph Theory (Elective)                            | PRIJA .V      | 5 |  |  |  |  |
|            | Name of Class Incharge   | PRIJA .V      |   |  |  |  |  |

### TIME TABLE

| Day | 09.50 Am -<br>10.45 Am | 10.45 Am -11.40<br>Am | 11.55 Am -12.50<br>Pm | 01.40 Pm -<br>02.35 Pm | 02.35 Pm -<br>03.30 Pm |
|-----|------------------------|-----------------------|-----------------------|------------------------|------------------------|
| 1   | Athulya P              | Prija V               | Anil M V              | Riya Baby              | Najumunnisa K          |
| 2   | Najumunnisa K          | Athulya P             | Prija V               | Anil M V               | Riya Baby              |
| 3   | Anil M V               | Athulya P             | Riya Baby             | Najumunnisa K          | Prija V                |
| 4   | Prija V                | Najumunnisa K         | Riya Baby             | Anil M V               | Athulya P              |
| 5   | Riya Baby              | Athulya P             | Najumunnisa K         | Prija V                | Anil M V               |

| Subject Code:         | MAT3C11       |
|-----------------------|---------------|
| Subject Name:         | Number Theory |
| No. of Credits:       | 4             |
| No. of Contact Hours: | 90            |
| Hours per Week:       | 5             |
| Name of the Teacher:  | Najumunnisa.K |

Text books

1. Tom M Apostol: Introduction to Analytic Number Theory; Springer International Student Editon

2. D.M Burton: Elementary Number Theory (6th Edition) Mc Graw Hill

3. lan Stewart and David Tall: Algebraic Number Theory and Fermal's last theorem (Third Edition) A K Peters Natick Massachussets

### Unit I

The Fundamental theorem of Arithmetic: Introduction-Divisibility-Greatest common divisor-

prime numbers- The fundamental theorem of arithmetic-The series of reciprocals of primes-

The Euclidean algorithm-The greatest common divisor of more than two numbers.

(Text 1, Sectons1.1-1.8)

Arithmetical Functions and Dirichlet multiplication: Introduction- The Mobius function  $\mu(n)$ 

–The Euler totient function  $\varphi$  (n) –The relation connecting  $\mu$  and  $\varphi$  -the product formula for

 $\phi$  (n) –The Dirichlet product of arithmetical functions- Dirichlet inverses and Mobius inversion formula- The Mangolt function  $\Lambda(n)$  –Multiplicative functions-Multiplicative

functions and Dirichlet multiplication- The inverse of a completely multiplicative function-

Liouville's function  $\lambda(n)$ - The divisor function  $\sigma\alpha(n)$ .

(Text 1, Section 2.1-2.13)

Congruences: Definition and basic properties of congruences- Residue classes and complete

residue system- Liner Congruences-Reduced residue system and the Euler- Fermat theorem-

Polynomial congruences modulo P and Langrange's theorem- Applications of Langrange's theorem- Simultaneous linear congruences and Chinese Remainder theorem-Applications of Chinese remainder theorem- Polynomial congruences with prime power moduli. (Text 1, Section 5.1-5.9)

Unit II

Quadratic Residues and Quadratic Reciprocity Law: Quadratic residues- Legendre's symbol and its properties- Evaluation of  $(-1 \Box p)$  and  $(2 \Box p)$  Gauss lemma-The quadratic reciprocity law – Applications of the reciprocity law – The Jacobi symbol-Applications to Diophantine equations. (Text 1, Sections 9.1–9.8)

Primitive Roots: The exponent of number mod m and primitive roots- Primitive roots and

reduced residu; system- The nonexistence of primitive roots mod 2a for  $\alpha \ge 3$ - The existence

of primitive roots mod  $\boldsymbol{p}$  for odd primes  $\boldsymbol{p}\text{-}$  Primitive roots and quadratic residues – The

existence of primitive roots and Pa

- The existence of primitive roots mod 2 Pa – The

nonexistence of Primitive roots in the remaining cases- The number of primitive roots mod

m.

(Text 1, Sections 10.1-10.9)

Introduction to Cryptography; From Caesar Cipher to Public Key Cryptography-The Knapsack Crypto system- An application of primitive roots to Cryptography. (Text 2, Sections 10.1-10.3)

Unit III

Algebraic Backgrounds: Symmetric polynomials- modules- free abelian groups (Text 3, Section 1.4-1.6)

Algebraic Numbers: Algebraic numbers- Conjugates and Discriminants- Algebraic integers-

Integral bases- Norms and Traces- Rings of integers.

(Text 3, Section 2.1-2.6)

Quadratic and Cyclotomic fields: Quadratic fields-Cyclotomic fields.

(Text 3, Sections 3.1-3.2)

| No of<br>Weeks | Dates            | Session   | Торіс  |
|----------------|------------------|-----------|--|
|                |                  | 1         | Introduction-Divisibility  |
|                | 04-07-2022       | 2         | Properties of divisibility   |
| 1              | То               | 3         | Greatest common divisor  |
|                | 08-07-2022       | 4         | Greatest common divisor  |
|                |                  | 5         | Theorem  |
|                |                  | 6         | Prime numbers  |
|                | 11-07-2022       | 7         | The fundamental theorem of arithmetic                                |
| 2              | То               | 8         | Theorem  |
|                | 15-07-2022       | 9         | The fundamental theorem of arithmetic                                |
|                |                  | 10        | The series of reciprocals of primes                                  |
|                | 18-07-2022       | 11        | Arithmetical Functions and Dirichlet multiplication:<br>Introduction |
| 2              |                  | 12        | The Mobius function $\mu(n)$   |
| 3              | То               | 13        | The Euler totient function $\phi$ (n)                                |
|                | 22-07-2022       | 14        | The relation connecting $\mu$ and $\phi$                             |
|                |                  | 15        | The product formula for $\phi(n)$                                    |
|                |                  | 16        | The Dirichlet product of arithmetical functions                      |
|                | 25-07-2022       | 17        | Dirichlet inverses and Mobius inversion formula                      |
| 4              | То               | 18        | Dirichlet inverses and Mobius inversion formula                      |
|                | 29-07-2022       | 28 July   | Karkidavav   |
|                |                  | 19        | Multiplicative functions   |
|                |                  | 20        | Examples   |
| _              | 01-08-2022       | 21        | Multiplicative<br>functions and Dirichlet multiplication             |
| 5              | То               | 22        | The inverse of a completely multiplicative function                  |
|                | 05-08-2022       | 23        | Liouville's function $\lambda(n)$                                    |
|                |                  | 24        | The divisor function $\sigma \alpha(n)$                              |
|                |                  | 08 August | Muharam  |
|                | 00 00 0000       | 25        | Definition and basic properties of congruences                       |
| 6              | 08-08-2022<br>To | 26        | Residue classes and complete residue system                          |
|                | 12-08-2022       | 27        | Residue classes and complete<br>residue system                       |
|                |                  | 28        | Linear Congrunces  |
| 7              | 15-08-2022       | 15 August | Independence Day   |
|                | 15-06-2022       | 29        | Euler- Fermat theorem  |

| No of<br>Weeks | Dates      | Session      | Торіс   |
|----------------|------------|--------------|---|
|                | То         | 30           | Polynomial congruences modulo P                               |
|                | 19-08-2022 | 18 August    | Sree Krishna Jayanthi   |
|                |            | 31           | Discussion  |
|                |            | 32           | I internal Examination  |
|                | 22-08-2022 | 33           | I internal Examination  |
| 8              | То         | 34           | I internal Examination  |
|                | 26-08-2022 | 35           | I internal Examination  |
|                |            | 36           | I internal Examination  |
|                |            | 37           | Applications of Langrange's theorem                           |
|                | 29-08-2022 | 38           | Simultaneous linear congruences                               |
| 9              | То         | 39           | Chinese Remainder theorem                                     |
|                | 02-09-2022 | 40           | Applications of<br>Chinese remainder theorem                  |
|                |            | 41           | Polynomial congruences with prime power moduli.               |
|                | 05-09-2022 | 05 September | ONAM VACATION   |
|                | То         | 06 September | ONAM VACATION   |
| 10             | 09-09-2022 | 07 September | ONAM VACATION   |
|                | 09-09-2022 | 08 September | ONAM VACATION   |
|                |            | 09 September | ONAM VACATION   |
|                |            | 42           | Quadratic residues  |
|                | 12.00.2022 | 43           | Legendre's  |
| 11             | 12-09-2022 | 44           | symbol and its properties-<br>Gauss lemma                     |
| 11             |            |              | The quadratic   |
|                | 16-09-2022 | 45           | reciprocity law   |
|                |            | 46           | Applications of the reciprocity law                           |
|                |            | 47           | The Jacobi symbol-  |
|                | 19-09-2022 | 48           | Theorems  |
| 12             | То         | 21 September | Sree Narayana Guru Samadhi                                    |
|                | 23-09-2022 | 49           | Applications to<br>Diophantine equations.                     |
|                |            | 50           | The exponent of number mod m and primitive roots              |
|                | 26-09-2022 | 51           | Primitive roots and<br>reduced residu; system                 |
| 13             | То         | 52           | The nonexistence of primitive roots mod 2a for $\alpha \ge 3$ |
| 10             | 30-09-2022 | 53           | The existence<br>of primitive roots mod p for odd primes p    |
|                |            | 54           | Primitive roots and quadratic residues                        |

| No of<br>Weeks | Dates      | Session    | Торіс                                |
|----------------|------------|------------|--------------------------------------|
|                |            | 55         | The number of primitive roots mod m. |
|                |            | 56         | Seminar                              |
|                | 03-10-2022 | 04 October | Mahanavami                           |
| 14             | То         | 05 October | Vijayadasami                         |
|                | 07-10-2022 | 57         | Seminar                              |
|                |            | 58         | Seminar                              |
|                |            | 59         | Seminar                              |
|                | 10-10-2022 | 60         | Norms and traces                     |
| 15             | То         | 61         | Rings of integers.                   |
|                | 14-10-2022 | 62         | Class Test                           |
|                |            | 63         | Quadratic fields                     |
|                |            | 64         | Theorems                             |
|                | 17-10-2022 | 65         | Symmetric polynomials                |
| 16             | То         | 66         | Symmetric polynomials                |
|                | 21-10-2022 | 67         | Modules                              |
|                |            | 68         | Modules                              |
|                |            | 24 October | Deepavali                            |
|                | 24-10-2022 | 69         | II Internal Examination              |
| 17             | То         | 70         | II Internal Examination              |
|                | 28-10-2022 | 71         | II Internal Examination              |
|                |            | 72         | II Internal Examination              |
|                | 21.0.2022  | 73         | Discussion                           |
| 10             | 31-0-2022  | 74         | Class Test                           |
| 18             | То         | 75         | free abelian group                   |
|                | 04-11-2022 | 76         | free abelian group                   |
|                |            | 77         | Algebraic numbers                    |
|                |            | 78         | Algebraic numbers                    |
| 10             | 07-11-2022 | 79         | Conjugates and Discriminant          |
| 19             | То         | 80         | Algebraic integers                   |
|                | 11-11-2022 | 81         | Integral bases                       |
|                |            | 82         | Norms and traces                     |
|                |            | 83         | III Semester University Examination  |
|                | 14-11-2022 | 84         | III Semester University Examination  |
| 20             | То         | 85         | III Semester University Examination  |
|                | 18-11-2022 | 86         | III Semester University Examination  |
|                |            | 87         | III Semester University Examination  |
| 01             | 01 11 0000 | 88         | III Semester University Examination  |
| 21             | 21-11-2022 | 89         | III Semester University Examination  |

| No of<br>Weeks | Dates      | Session | Торіс                               |
|----------------|------------|---------|-------------------------------------|
|                | То         | 90      | III Semester University Examination |
|                | 25-12-2022 |         |                                     |
|                |            |         |                                     |
|                |            |         |                                     |
|                |            |         |                                     |

| Subject Code:         | MAT3C12             |
|-----------------------|---------------------|
| Subject Name:         | Functional Analysis |
| No. of Credits:       | 4                   |
| No. of Contact Hours: | 90                  |
| Hours per Week:       | 5                   |
| Name of the Teacher:  | Anil M V            |

### MAT3C12: FUNCTIONAL ANALYSIS

### Unit I

Fundamentals of Normed Spaces; Normed Spaces, Continuity of Linear Maps, Hahn-Banach Theorems, Banach spaces.

(Chapter-2, Sections 5, 6, 7 and 8 [omitting Banach Limits from Section 7])

### Unit II

Bounded Linear Maps on Banach Spaces; Uniform Boundedness Principle, Closed Graph and Open Mapping Theorems, Bounded Inverse Theorem

(Chapter-3, Sections 9, 10 and 11, Omitting Divergence of Fourier Series of Continuous Functions, Quadrature Formula and Matrix Transformation and Summability Methods of Section 9)

### Unit III

Geometry of Hilbert Spaces; Inner Product Spaces, Orthonormal Sets. Approximation and Optimization, Projection and Riesz Representation Theorems.

(Chapter-6, Sections 21, 22, 23 and 24 [Omit 23.2, 23.6 from section 23 and Weak Convergence and Weak Boundedness from Section 24]

Text Book; Balmohan V Limaye; Functional Analysis (Third Edition); New Age International Publishers.

Reference:

- 1. E.Kreyszig; Introductory Functional Analysis with Applications, John Wiley
- 2. Walter Rudin; Functional Analysis, TMH Editons 1978
- 3. M.T Nair; Functional Analysis A First Course; Prentice Hall of India.

4. Chaudhary and Sudarsan Nanda; Functional Analysis with Applications, Wiley Eastern Ltd.

5. Walter Rudin; Introduction to Real and Complex Analysis, McGraw Hill International Edition

- 6. J.B Conway; Functional Analysis, Narosa Publishing Company
- 7. Bachman and Narici; Functional Analysis

| No of<br>Weeks | Dates      | Session   | Торіс                                 |
|----------------|------------|-----------|---------------------------------------|
|                |            | 1         | Fundamentals of normed spaces         |
|                | 04-07-2022 | 2         | Normed spaces-definition and examples |
| 1              | То         | 3         | Properties of normed spaces           |
|                | 08-07-2022 | 4         | Properties of normed spaces           |
|                |            | 5         | Examples of normed spaces             |
|                |            | 6         | Theorem                               |
|                | 11-07-2022 | 7         | Riesz lemma                           |
| 2              | То         | 8         | Theorem                               |
|                | 15-07-2022 | 9         | Theorem                               |
|                |            | 10        | Definitions                           |
|                |            | 11        | Theorem                               |
|                | 18-07-2022 | 12        | Continuity of linear maps             |
| 3              | То         | 13        | Theorem                               |
|                | 22-07-2022 | 14        | Theorem                               |
|                |            | 15        | Bounded linear maps                   |
|                |            | 16        | Lemma                                 |
|                | 25-07-2022 | 17        | Lemma                                 |
| 4              | То         | 18        | Hahn Banach separation theorem        |
|                | 29-07-2022 | 28 July   | Karkidaka Vav                         |
|                |            | 19        | Class test                            |
|                | 01.00.0000 | 20        | Hahn Banach Extension theorem         |
|                | 01-08-2022 | 21        | Banach spaces                         |
| 5              | То         | 22        | Characterization of Banach spaces     |
|                | 05-08-2022 | 23        | Theorem                               |
|                |            | 24        | Theorem                               |
|                | 00.00.0000 | 08 August | Muharam                               |
| -              | 08-08-2022 | 25        | Embedding a normed space              |
| 6              | То         | 26        | Theorem                               |
|                | 12-08-2022 | 27        | Bounded linear maps on Banach spaces  |
|                |            | 28        | Uniform boundedness principle         |
|                | 15 09 2022 | 15 August | Independence Day                      |
| _              | 15-08-2022 | 29        | Resonance theorem                     |
| 7              | To         | 30        | Corollary                             |
|                | 19-08-2022 | 18 August | Sree Krishna Jayanthi                 |
|                |            | 31        | Closed map                            |

| No of<br>Weeks | Dates      | Session      | Торіс                      |
|----------------|------------|--------------|----------------------------|
|                |            | 32           | I internal Examination     |
|                | 22-08-2022 | 33           | I internal Examination     |
| 8              | То         | 34           | I internal Examination     |
|                | 26-08-2022 | 35           | I internal Examination     |
|                |            | 36           | I internal Examination     |
|                |            | 37           | Examples                   |
|                | 29-08-2022 | 38           | Examples                   |
| 9              | То         | 39           | Lemma                      |
|                | 02-09-2022 | 40           | Closed graph theorem       |
|                |            | 41           | Open map                   |
|                | 05-09-2022 | 05 September | ONAM VACATION              |
|                | То         | 06 September | ONAM VACATION              |
| 10             | 09-09-2022 | 07 September | ONAM VACATION              |
|                |            | 08 September | ONAM VACATION              |
|                |            | 09 September | ONAM VACATION              |
|                |            | 42           | Theorem                    |
|                | 12-09-2022 | 43           | Corollary                  |
| 11             | То         | 44           | Projection maps            |
|                | 16-09-2022 | 45           | Open map                   |
|                |            | 46           | Theorem                    |
|                |            | 47           | Examples                   |
|                | 19-09-2022 | 48           | Examples                   |
| 12             | То         | 21 September | Sree Narayana Guru Samadhi |
|                | 23-09-2022 | 49           | Class test                 |
|                |            | 50           | Definitions                |
|                |            | 51           | Theorem                    |
|                | 26-09-2022 | 52           | Theorem                    |
| 13             | То         | 53           | Definitions                |
|                | 30-09-2022 | 54           | Open mapping therorem      |
|                |            | 55           | Examples                   |
|                | 02 10 2022 | 56           | Bounded inverse theorem    |
| 14             | 03-10-2022 | 04 October   | Mahanavami                 |
| 14             | To         | 05 October   | Vijayadasami               |
|                | 07-10-2022 | 57           | Examples                   |
|                |            | 58           | Two norm theorem           |
| 15             | 10-10-2022 | 59<br>60     | Examples<br>Class test     |
|                |            | 60           | Class test                 |

| No of | Dates      | Session    | Торіс                                   |
|-------|------------|------------|---|
| Weeks |            |            |   |
|       | То         | 61         | Inner product spaces                    |
|       | 14-10-2022 | 62         | Seminar                                 |
|       |            | 63         | Seminar                                 |
|       | 17 10 2022 | 64         | Seminar                                 |
| 1.5   | 17-10-2022 | 65         | Seminar                                 |
| 16    | То         | 66         | Seminar                                 |
|       | 21-10-2022 | 67         | Seminar                                 |
|       |            | 68         | Seminar                                 |
|       | 24 10 2022 | 24 October | Deepavali                               |
|       | 24-10-2022 | 69         | II Internal Examination                 |
| 17    | То         | 70         | II Internal Examination                 |
|       | 28-10-2022 | 71         | II Internal Examination                 |
|       |            | 72         | II Internal Examination                 |
|       | 21.0.2022  | 73         | Hilbert spaces                          |
| 10    | 31-0-2022  | 74         | Theorem                                 |
| 18    | То         | 75         | Lemma                                   |
|       | 04-11-2022 | 76         | Theorem                                 |
|       |            | 77         | Theorem                                 |
|       |            | 78         | Examples                                |
| 10    | 07-11-2022 | 79         | Projection theorem                      |
| 19    | То         | 80         | Riez representation theorem<br>Revision |
|       | 11-11-2022 | 81         |   |
|       |            | 82         | Revision                                |
|       |            | 83         | III Semester University Examination     |
|       | 14-11-2022 | 84         | III Semester University Examination     |
| 20    | То         | 85         | III Semester University Examination     |
|       | 18-11-2022 | 86         | III Semester University Examination     |
|       | 10 11 2022 | 87         | III Semester University Examination     |
|       |            | 88         | III Semester University Examination     |
|       |            | 89         | III Semester University Examination     |
|       | 21-11-2022 | 90         | III Semester University Examination     |
| 21    | То         |            |   |
|       | 25-12-2022 |            |   |
|       |            |            |   |
|       |            |            |   |

| Subject Code:         | MAT3C13                 |
|-----------------------|-------------------------|
| Subject Name:         | Complex function theory |
| No. of Credits:       | 4                       |
| No. of Contact Hours: | 90                      |
| Hours per Week:       | 5                       |
| Name of the Teacher:  | RIYA BABY               |

### **Syllabus**

Unit I:

Elliptic functions: Simple periodic functions, doubly periodic functions, the Weierstrass theory. ( Chapter 7 ( sections 1,2,3) of text 1 ). The Reimann zeta function (chapter 7( section 8) of text 2).

#### Unit II:

Runge's theorem, simple connectedness, Mittag-Leffler's theorem. Analytic Continuation and Riemann surfaces: Schwartz reflection principle, analytic continuation along a path, monodrama theorem.

(Chapter 8 (sections 1,2,3) and chapter 9 (sections 1,2,3) of text 2)

### Unit III:

Harmonic functions: Basic properties of harmonic functions, Harmonic functions on a disk, sub- harmonic and super harmonic functions. Entire functions: Jensen's formula.

(Chapter 10 (sections 1,2,3), chapter 11 (section 1) of text 2).

Text 1: Lars V Ahlfors- Complex Analysis 3rd edition Text 2: John B Coway- Functions of one complex variable 2nd edition.

| No of<br>Weeks | Dates            | Session   | Торіс                                     |
|----------------|------------------|-----------|---|
|                |                  | 1         | Introduction to simply periodic functions |
|                | 04-07-2022       | 2         | Representation of exponentials            |
| 1              | То               | 3         | The Fourier development                   |
|                | 08-07-2022       | 4         | Functions of finite orders                |
|                |                  | 5         | Examples                                  |
|                |                  | 6         | Doubly periodic functions                 |
|                | 11-07-2022       | 7         | Period module                             |
| 2              | То               | 8         | Theorem 1                                 |
|                | 15-07-2022       | 9         | Theorem 1                                 |
|                |                  | 10        | Unimodular transformation                 |
|                |                  | 11        | Class test                                |
|                | 18-07-2022       | 12        | Theorem 2                                 |
| 3              | То               | 13        | Theorem 2                                 |
|                | 22-07-2022       | 14        | General properties of elliptic functions  |
|                |                  | 15        | Theorem 3                                 |
|                |                  | 16        | Theorem                                   |
|                | 25-07-2022       | 17        | Theorem                                   |
| 4              | To<br>29-07-2022 | 18        | Theorem 3                                 |
|                |                  | 28 July   | Karkidaka Vav                             |
|                |                  | 19        | The Weierstrass P function                |
|                |                  | 20        | Properties of Weierstrass P function      |
|                | 01-08-2022       | 21        | Legender's relation                       |
| 5              | То               | 22        | Differential equations                    |
|                | 05-08-2022       | 23        | Reimann zeta function                     |
|                |                  | 24        | Properties of Riemann zeta function       |
|                |                  | 08 August | Muharam                                   |
|                | 08-08-2022       | 25        | Lemma 8.3                                 |
| 6              | То               | 26        | Lemma 8.3                                 |
|                | 12-08-2022       | 27        | Corollary 8.4                             |
|                |                  | 28        | Sigma function                            |
|                | 15-08-2022       | 15 August | Independence Day                          |
| 7              | To               | 29        | Proposition 8.5                           |
|                |                  | 30        | Riemann functional equation               |

| No of<br>Weeks | Dates      | Session      | Торіс                                       |
|----------------|------------|--------------|---|
|                | 19-08-2022 | 18 August    | Sree Krishna Jayanthi                       |
|                |            | 31           | Harnack' s inequality and Harnack's theorem |
|                |            | 32           | I internal Examination                      |
|                | 22-08-2022 | 33           | I internal Examination                      |
| 8              | То         | 34           | I internal Examination                      |
|                | 26-08-2022 | 35           | I internal Examination                      |
|                |            | 36           | I internal Examination                      |
|                |            | 37           | Theorem                                     |
|                | 29-08-2022 | 38           | Riemann hypothesis                          |
| 9              | То         | 39           | Euler's theorem                             |
|                | 02-09-2022 | 40           | Class test                                  |
|                |            | 41           | Lemma 1.8                                   |
|                | 05-09-2022 | 05 September | ONAM VACATION                               |
|                | To         | 06 September | ONAM VACATION                               |
| 10             |            | 07 September | ONAM VACATION                               |
|                | 09-09-2022 | 08 September | ONAM VACATION                               |
|                |            | 09 September | ONAM VACATION                               |
|                |            | 42           | Proposition 1.1                             |
|                | 12-09-2022 | 43           | Lemma 1.5                                   |
| 11             | То         | 44           | Runge's theorem                             |
|                | 16-09-2022 | 45           | Lemma 1.9                                   |
|                |            | 46           | Lemma 1.10                                  |
|                |            | 47           | Corollary 1.14                              |
|                | 19-09-2022 | 48           | Corollary 1.15                              |
| 12             | То         | 21 September | Sree Narayana Guru Samadhi                  |
|                | 23-09-2022 | 49           | Polynomially convex hull                    |
|                |            | 50           | Homeomorphic sets                           |
|                |            | 51           | Theorem 2.2                                 |
|                | 26-09-2022 | 52           | Mittag- Loffler's theorem                   |
| 13             | То         | 53           | Mittag- Loffler's theorem                   |
|                | 30-09-2022 | 54           | Schwartz reflection principle               |
|                |            | 55           | Schwartz reflection principle               |
|                |            | 56           | Schwartz reflection principle               |
|                | 03-10-2022 | 04 October   | Mahanavami                                  |
| 14             | То         | 05 October   | Vijayadasami                                |
|                | 07-10-2022 | 57           | Analytic continuation along a path          |
|                |            | 58           | Analytic continuation along a path          |

| No of<br>Weeks | Dates                         | Session    | Торіс                                 |
|----------------|-------------------------------|------------|---------------------------------------|
|                | 10-10-2022                    | 59         | Function element                      |
|                |                               | 60         | Proposition 2.4                       |
| 15             | То                            | 61         | Lemma 3.1                             |
|                | 14-10-2022                    | 62         | Lemma 3.2                             |
|                |                               | 63         | Monodromy theorem                     |
|                |                               | 64         | Monodromy theorem                     |
|                | 17-10-2022                    | 65         | Corollary 3.9                         |
| 16             | То                            | 66         | Class test                            |
|                | 21-10-2022                    | 67         | Basic properties of harmonic function |
|                |                               | 68         | Basic properties of harmonic function |
|                |                               | 24 October | Deepavali                             |
|                | 24-10-2022                    | 69         | II Internal Examination               |
| 17             | То                            | 70         | II Internal Examination               |
|                | 28-10-2022                    | 71         | II Internal Examination               |
|                |                               | 72         | II Internal Examination               |
|                | 31-0-2022<br>To<br>04-11-2022 | 73         | Mean value theorem                    |
|                |                               | 74         | Maximum principle first version       |
| 18             |                               | 75         | Maximum principle second version      |
|                |                               | 76         | Maximum principle second version      |
|                |                               | 77         | Corollary 1.9                         |
|                |                               | 78         | Minimum principle                     |
|                | 07-11-2022                    | 79         | Poisson kernel                        |
| 19             | To<br>11-11-2022              | 80         | Revision                              |
|                |                               | 81         | Revision                              |
|                |                               | 82         | Revision                              |
|                |                               | 83         | III Semester University Examination   |
|                | 14-11-2022                    | 84         | III Semester University Examination   |
| 20             | To                            | 85         | III Semester University Examination   |
|                | 18-11-2022                    | 86         | III Semester University Examination   |
|                | 10 11 2022                    | 87         | III Semester University Examination   |
|                |                               | 88         | III Semester University Examination   |
|                |                               | 89         | III Semester University Examination   |
|                | 21-11-2022                    | 90         | III Semester University Examination   |
| 21             | То                            |            |                                       |
|                | 25-12-2022                    |            |                                       |
|                |                               |            |                                       |
|                |                               |            |                                       |

| Subject Code:         | MAT3C14                |
|-----------------------|------------------------|
| Subject Name:         | ADVANCED REAL ANALYSIS |
| No. of Credits:       | 4                      |
| No. of Contact Hours: | 90                     |
| Hours per Week:       | 5                      |
| Name of the Teacher:  | ATHULYA P              |

#### MAT3C14: ADVANCED REAL ANALYSIS

Text Book: Walter Rudin: Principles of Mathematical Analysis; (3rd Edition) Mc. Graw Hill,

1986.

Unit I

Sequence and series of Functions: Discussion of Main Problem, Uniform Convergence,

Uniform Convergence Continuity, Uniform Convergence and Integration, Uniform Convergence and Differentiation, Equicontinous Family of Functions, The Stone-Weierstrass

Theorem,

(Chapter-7; Sections 7.1 to 7.33 and Theorem 7.33)

Unit II

Some Special Functions; Power Series, The Exponential and Logarithmic Functions, The

Trigonometric Functions, The Algebraic Completeness of the Complex Field, Fourier Series.

The Gamma Function

(Chapter-8: Sections 8.1 to 8.22)

Unit III

Functions of Several Variables: Liner Transformations, Differentiation The Contraction

Principle, The Inverse Function Theorem, The Implicit Function Theorem,

(Chater-9; Sections 9.1 to 9.29

| No of<br>Weeks | Dates      | Session   | Торіс                                       |
|----------------|------------|-----------|---|
|                |            | 1         | Introduction                                |
|                | 04-07-2022 | 2         | Sequence and series of Functions            |
| 1              | То         | 3         | Pointwise convergence                       |
|                | 08-07-2022 | 4         | Pointwise convergence                       |
|                |            | 5         | Examples                                    |
|                |            | 6         | Interchange of limit                        |
|                | 11-07-2022 | 7         | Examples                                    |
| 2              | То         | 8         | Examples                                    |
|                | 15-07-2022 | 9         | Formal Definition of pointwise convergence. |
|                |            | 10        | Discussion of Main Problem                  |
|                |            | 11        | Uniform convergence                         |
|                | 18-07-2022 | 12        | Cauchy criterion for uniform convergence    |
| 3              | То         | 13        | Theorem                                     |
|                | 22-07-2022 | 14        | Definition                                  |
|                |            | 15        | Weierstrass-M Test                          |
|                |            | 16        | Examples                                    |
|                | 25-07-2022 | 17        | Examples                                    |
| 4              | То         | 18        | Examples                                    |
|                | 29-07-2022 | 28 July   | Karkidaka Vav                               |
|                |            | 19        | Assignment                                  |
|                |            | 20        | Uniform Convergence and Continuity          |
|                | 01-08-2022 | 21        | Theorem                                     |
| 5              | То         | 22        | Theorem                                     |
|                | 05-08-2022 | 23        | Definition                                  |
|                |            | 24        | Theorem                                     |
|                |            | 08 August | Muharam                                     |
|                | 08-08-2022 | 25        | Theorem                                     |
| 6              | То         | 26        | Class test                                  |
|                | 12-08-2022 | 27        | Uniform Convergence and Integration         |
|                |            | 28        | Theorem                                     |
|                | 15 00 2022 | 15 August | Independence Day                            |
|                | 15-08-2022 | 29        | Corollary                                   |
| 7              | То         | 30        | Uniform Convergence and Differentiation     |
|                | 19-08-2022 | 18 August | Sree Krishna Jayanthi                       |
|                |            | 31        | Theorem                                     |

| No of<br>Weeks | Dates      | Session                  | Торіс   |
|----------------|------------|--------------------------|---|
|                | 22-08-2022 | 32                       | I internal Examination                                    |
|                |            | 33                       | I internal Examination                                    |
| 8              | То         | 34                       | I internal Examination                                    |
|                | 26-08-2022 | 35                       | I internal Examination                                    |
|                |            | 36                       | I internal Examination                                    |
|                |            | 37                       | Theorem   |
|                | 29-08-2022 | 38                       | Theorem   |
| 9              | То         | 39                       | Examples  |
|                | 02-09-2022 | 40                       | Equicontinous Family of Functions                         |
|                |            | 41                       | Equicontinous Family of Functions                         |
|                | 05-09-2022 | 05 September             | ONAM VACATION   |
|                | То         | 06 September             | ONAM VACATION   |
| 10             | 09-09-2022 | 07 September             | ONAM VACATION   |
|                | 07 07 2022 | 08 September             | ONAM VACATION   |
|                |            | 09 September             | ONAM VACATION   |
|                |            | 42                       | Pointwise Bounded   |
|                | 12-09-2022 | 43                       | Uniform Bounded   |
| 11             | То         | 44                       | Examples  |
|                | 16-09-2022 | 45                       | Examples  |
|                |            | 46                       | Class test  |
|                |            | 47                       | Equicontinous Functions                                   |
|                | 19-09-2022 | 48                       | Theorem   |
| 12             | То         | 21 September             | Sree Narayana Guru Samadhi                                |
|                | 23-09-2022 | 49                       | Theorem   |
|                |            | 50                       | The Stone-Weierstrass Theorem                             |
|                |            | 51                       | Introduction  |
| 10             | 26-09-2022 | 52                       | Some Special Functions                                    |
| 13             | То         | 53                       | Theorem   |
|                | 30-09-2022 | 54                       | Theorem   |
|                |            | 55                       | Power Series  |
|                | 03-10-2022 | 56                       | Examples  |
| 14             |            | 04 October<br>05 October | Mahanavami  |
| 14             | To         | 57                       | Vijayadasami<br>The Exponential and Logarithmic Functions |
|                | 07-10-2022 | 58                       | The Exponential and Logarithmic Functions                 |
|                |            | 59                       | Theorem   |
| 15             | 10-10-2022 | 60                       | Theorem   |
|                |            | 00                       |   |

| No of<br>Weeks | Dates            | Session    | Торіс   |
|----------------|------------------|------------|---|
|                | То               | 61         | The Trigonometric Functions                     |
|                | 14-10-2022       | 62         | The Algebraic Completeness of the Complex Field |
|                |                  | 63         | The Algebraic Completeness of the Complex Field |
|                |                  | 64         | Assignment                                      |
|                | 17-10-2022       | 65         | Class test                                      |
| 16             | То               | 66         | Fourier Series                                  |
|                | 21-10-2022       | 67         | Examples  |
|                |                  | 68         | The Gamma Function                              |
|                |                  | 24 October | Deepavali                                       |
|                | 24-10-2022       | 69         | II Internal Examination                         |
| 17             | То               | 70         | II Internal Examination                         |
|                | 28-10-2022       | 71         | II Internal Examination                         |
|                |                  | 72         | II Internal Examination                         |
|                |                  | 73         | Examples  |
|                | 31-0-2022        | 74         | The Contraction Principle                       |
| 18             | To<br>04-11-2022 | 75         | Examples  |
|                |                  | 76         | Assignment                                      |
|                |                  | 77         | The Inverse Function Theorem                    |
|                |                  | 78         | The Implicit Function Theorem                   |
|                | 07 11 2022       | 79         | Class test                                      |
| 19             | 07-11-2022       | 80         | Revision  |
|                | То               | 81         | Revision  |
|                | 11-11-2022       | 82         | Revision  |
|                |                  | 83         | III Semester University Examination             |
|                | 14-11-2022       | 84         | III Semester University Examination             |
| 20             | То               | 85         | III Semester University Examination             |
| 20             | 18-11-2022       | 86         | III Semester University Examination             |
|                | 10-11-2022       | 87         | III Semester University Examination             |
|                |                  | 88         | III Semester University Examination             |
|                |                  | 89         | III Semester University Examination             |
|                | 21-11-2022       | 90         | III Semester University Examination             |
| 21             | То               |            |   |
|                | 25-12-2022       |            |   |
|                |                  |            |   |
|                |                  |            |   |

| Subject Code:         | MAT3E01                 |  |
|-----------------------|-------------------------|--|
| Subject Name:         | Graph Theory (Elective) |  |
| No. of Credits:       | 4                       |  |
| No. of Contact Hours: | 90                      |  |
| Hours per Week:       | 5                       |  |
| Name of the Teacher:  | Prija V                 |  |

#### MAT3E01: Elective Graph Theory (Elective)

Text 1 J.A Bondy and U.S Murty, Graph Theory with Applications, The MacMillan Press Ltd, 1976 Text 2 John Clark and Derek Allan Holtan, A First Look at Graph Theory, Allied Publishers, Ltd

#### Unit I

Independent Sets and Cliques; Independent Sets, Ramsey's Theorem, Turan's Theorem, Shur's Theorem Vertex Colorings: Chromatic Number, Book's Theorem Hajo's Conjecture, Chromatic Polynomials, Girth and Chromatic Number. (Chapter 7; Except Section 7.5, Chapter 8 Except Section 8.6, Text 1)

#### Unit II

Edge Colourings: Edge Chromatic Number, Vizing's Theorem, The Timetabling Problem Planar Graphs; Plane and Planar Graphs, Dual Graphs, Euler's Formula Bridges, Kuratowski's Theorem. The Five Colour Theorem Non Hamiltonian Planar Graphs. (Chapter 6, All sections; Chapter 9; Except section 9.8 of Text 1)

#### Unit III

Matchings: Matchings, Matchings and Coverings in bipartite Graphs, Perfect Matchings, The Personnel Assignment Problem, The Optimal Assignment Problem. (Chapter 5, Sections 5.1, 5.2, 5.3, 5.4, 5.5 of text 1) Networks; Flows and Cuts, Separating sets (Chapter 8; Sections 8.1 & 8.3 of text 2

| No of<br>Weeks | Dates      | Session | Торіс                                      |
|----------------|------------|---------|--|
|                |            | 1       | Unit I-Introduction.                       |
|                | 04-07-2022 | 2       | Independent Sets –Definition and examples. |
| 1              | То         | 3       | Cliques–Definition and examples            |
|                | 08-07-2022 | 4       | Examples                                   |
|                |            | 5       | Assignment                                 |
| 2              | 11-07-2022 | 6       | Theorem .                                  |
| 2              | 11-07-2022 | 7       | Class test.                                |

| No of<br>Weeks | Dates      | Session   | Торіс   |
|----------------|------------|-----------|---|
|                | То         | 8         | Ramsey's Theorem.                               |
|                | 15-07-2022 | 9         | Corollary.                                      |
|                |            | 10        | Theorem .                                       |
|                |            | 11        | Theorem .                                       |
|                | 18-07-2022 | 12        | Turan's Theorem.                                |
| 3              | То         | 13        | Assignment                                      |
|                | 22-07-2022 | 14        | Corollary.                                      |
|                |            | 15        | Shur's Theorem.                                 |
|                |            | 16        | Corollary.                                      |
|                | 25-07-2022 | 17        | Theorem .                                       |
| 4              | То         | 18        | Exercises questions.                            |
|                | 29-07-2022 | 28 July   | Karkidaka Vav                                   |
|                |            | 19        | Corollary.                                      |
|                |            | 20        | Theorem .                                       |
|                | 01-08-2022 | 21        | Seminar.  |
| 5              | То         | 22        | Class test.                                     |
|                | 05-08-2022 | 23        | Vertex Colorings Definition and examples.       |
|                |            | 24        | Chromatic Number Definition and examples.       |
|                |            | 08 August | Muharam   |
|                | 08-08-2022 | 25        | Book's Theorem                                  |
| 6              | То         | 26        | Hajo's Conjecture                               |
|                | 12-08-2022 | 27        | Girth and Chromatic Number                      |
|                |            | 28        | Assignment                                      |
|                |            | 15 August | Independence Day                                |
|                | 15-08-2022 | 29        | Chromatic Polynomials- Definition and examples. |
| 7              | То         | 30        | Class test.                                     |
|                | 19-08-2022 | 18 August | Sree Krishna Jayanthi                           |
|                |            | 31        | Unit II-Introduction.                           |
|                |            | 32        | I internal Examination                          |
|                | 22-08-2022 | 33        | I internal Examination                          |
| 8              | То         | 34        | I internal Examination                          |
|                | 26-08-2022 | 35        | I internal Examination                          |
|                |            | 36        | I internal Examination                          |
|                |            | 37        | Edge Colourings -Definition and examples.       |
|                | 29-08-2022 | 38        | Edge Chromatic Number -Definition and examples. |
| 9              | То         | 39        | Vizing's Theorem.                               |
|                | 02-09-2022 | 40        | Corollary.                                      |
|                |            | 41        | Theorem .                                       |

| No of<br>Weeks | Dates            | Session      | Торіс   |
|----------------|------------------|--------------|---|
|                | 05-09-2022<br>To | 05 September | ONAM VACATION   |
| 10             |                  | 06 September | ONAM VACATION   |
|                |                  | 07 September | ONAM VACATION   |
|                | 09-09-2022       | 08 September | ONAM VACATION   |
|                |                  | 09 September | ONAM VACATION   |
|                |                  | 42           | The Timetabling Problem                                 |
|                | 12-09-2022       | 43           | Exercises questions.                                    |
| 11             | То               | 44           | Planar Graphs-Definition and examples.                  |
|                | 16-09-2022       | 45           | Plane and Planar Graphs.                                |
|                |                  | 46           | Theorem .   |
|                |                  | 47           | Theorem .   |
|                | 19-09-2022       | 48           | Dual Graphs-Definition and examples.                    |
| 12             | То               | 21 September | Sree Narayana Guru Samadhi                              |
|                | 23-09-2022       | 49           | Euler's Formula   |
|                |                  | 50           | Theorem .   |
|                |                  | 51           | Bridges- Definition and examples.                       |
|                | 26-09-2022       | 52           | Theorem .   |
| 13             | To<br>30-09-2022 | 53           | Assignment.   |
|                |                  | 54           | Seminar.  |
|                |                  | 55           | Kuratowski's Theorem.                                   |
|                | 02 10 2022       | 56           | The Five Colour Theorem.                                |
|                | 03-10-2022       | 04 October   | Mahanavami  |
| 14             | То               | 05 October   | Vijayadasami  |
|                | 07-10-2022       | 57           | Non Hamiltonian Planar Graphs -Definition and examples. |
|                |                  | 58           | Theorem.  |
|                | 10-10-2022<br>To | 59           | Class Test.   |
| 1.             |                  | 60           | Unit III-introduction.                                  |
| 15             |                  | 61           | Matchings-Definition and examples                       |
|                | 14-10-2022       | 62           | Matchings and Coverings in bipartite Graphs.            |
|                |                  | 63           | Definition and examples                                 |
|                | 17 10 2022       | 64           | Theorem.  |
| 10             | 17-10-2022<br>To | 65           | Theorem .   |
| 16             | To               | 66           | Perfect Matchings- Definition and examples              |
|                | 21-10-2022       | 67           | Theorem .   |
|                |                  | 68           | Assignment.   |
| 17             | 24-10-2022       | 24 October   | Deepavali   |
|                | _ 10 2022        | 69           | II Internal Examination                                 |

| No of<br>Weeks | Dates                          | Session | Торіс                                    |
|----------------|--------------------------------|---------|--|
|                | То                             | 70      | II Internal Examination                  |
|                | 28-10-2022                     | 71      | II Internal Examination                  |
|                |                                | 72      | II Internal Examination                  |
| 18             | 31-0-2022<br>To<br>04-11-2022  | 73      | The Personnel Assignment Problem.        |
|                |                                | 74      | Definition and examples                  |
|                |                                | 75      | Class Test.                              |
|                |                                | 76      | The Optimal Assignment Problem.          |
|                |                                | 77      | Theorem.                                 |
| 19             | 07-11-2022<br>To<br>11-11-2022 | 78      | Networks; Flows and Cuts.                |
|                |                                | 79      | Definition and examples                  |
|                |                                | 80      | Theorem.                                 |
|                |                                | 81      | Separating sets- Definition and examples |
|                |                                | 82      | Class test.                              |
| 20             | 14-11-2022<br>To<br>18-11-2022 | 83      | Revision.                                |
|                |                                | 84      | III Semester University Examination      |
|                |                                | 85      | III Semester University Examination      |
|                |                                | 86      | III Semester University Examination      |
|                |                                | 87      | III Semester University Examination      |
|                |                                | 88      | III Semester University Examination      |
| 21             | 21-11-2022<br>To<br>25-12-2022 | 89      | III Semester University Examination      |
|                |                                | 90      | III Semester University Examination      |
|                |                                |         |  |
|                |                                |         |  |
|                |                                |         |  |
|                |                                |         |  |