First Semester FYUGP Degree Supplementary Examination January 2025

KU1DSCMAT113 - FUNCTIONS, CALCULUS AND MATRICES

2024 Admission onwards

Time: 2 hours

Maximum Marks: 70

Section A

Answer any 6 questions. Each carry 3 marks.

- 1. Simplify and obtain the value of expression $2\ln(\sqrt{e})$.
- 2. Simplify the expression for $e^{-\ln x^2}$.
- 3. Using Sandwich theorem, prove that $\lim_{\theta \to 0} \sin \theta = 0$.
- 4. Differentiate $\sin(x^2 + e^x)$ with respect to x.
- 5. Find $\frac{d}{dx}(3^{-x})$
- 6. Find $\frac{d}{dx}(3^x)$.
- 7. Obtain $\int \sqrt[3]{x^2} dx$
- 8. Evaluate $\int_{1}^{2} \frac{1}{x} dx$

Section B

Answer any 4 questions. Each carry 6 marks.

- 9. Investment companies often use the model $y = Pe^{rt}$ in calculating the growth of an investment. Use this model to track the growth of \$100 invested in 2000 at an annual interest rate of 5.5%.
- 10. Calculate the value of the limit $\lim_{v\to 2} \frac{v^2-4}{v^4-16}$.
- 11. Simplify: $\ln(\cosh x + \sinh x) + \ln(\cosh x \sinh x)$.
- 12. Find an equation for a line that is tangent to the graph of $y = e^x$ and goes through the origin.
- 13. Evaluate $\lim_{x \to \pi/2} \cos \left(2x + \sin \left(\frac{3\pi}{2} + x\right)\right)$.

14. Find
$$\frac{dy}{dx}$$
 if $y = \cos(\ln x)$.

Section C

Answer any 2 questions. Each carry 14 marks.

15. If
$$A = \begin{bmatrix} 1 & 2 & 3 \\ 3 & -2 & 1 \\ 4 & 2 & 1 \end{bmatrix}$$
, compute $adjA$ and A^{-1} .

- 16. Use Gauss-Jordan method to find the inverse of the matrix $\begin{bmatrix} 2 & 1 & -1 \\ 0 & 2 & 1 \\ 5 & 2 & -3 \end{bmatrix}.$ 17. (a) Evaluate $\int_0^1 \frac{x^5}{1+x^{12}} dx.$ (b) Evaluate $\int \csc x \, dx.$