



K15P 0534

Reg. No. :

Name :

Third Semester M.C.A. Degree (Reg./Supple./Improve.)

Examination, January 2016

(2014 Admn.)

MCA3C15 : THEORY OF COMPUTATION

Time : 3 Hours

Max. Marks : 80

- Instructions :**
- 1) Answer **any ten** questions from Section – A. Each question carries **three** marks.
 - 2) Answer **all** questions from Section – B. Each question carries **10** marks.

SECTION – A

Note : Answer **any ten** questions from the following. Each question carries **three** marks. (10×3=30)

1. a) What is the difference between DFA and NFA ?
b) Design DFA to accept strings over $\Sigma = (0,1)$ with two consecutive 0's.
c) Construct a parse tree of $(a + b)^*c$ for the grammar
 $E \rightarrow E + E / E * E / (E) / id$.
d) Define CFG.
e) What is meant by empty production removal in PDA ?
f) Define the instantaneous description of PDA.
g) Write a note on Non-deterministic PDA.
h) Define Turing Machine Halting Problem.
i) Write a note on closure properties for CFL.
j) State pumping lemma for regular languages.
k) What is post correspondence problem ?
l) When a language is said to be recursively enumerable ?

P.T.O.

SECTION - B

Note : Answer all the questions. Each question carries ten marks. (5x10=

2. a) Design a DFA to accept language with even number of a's and odd number of b's over $L = \{a, b\}$ and process the string $U = aaaabbb$.
 b) Convert the following ϵ -NFA to DFA.



OR

3. a) Design a DFA to accept the following languages :
 i) Language having set of all string on the alphabet $\Sigma = \{0, 1\}$ that either begins or ends or both with substring '01'.
 ii) $L = \{(0, 1)^i 1^{2j} \mid i \geq 1, j \geq 1\}$
 b) Write a short note on the applications of Finite Automata.
4. a) Prove that the following are not regular languages.
 i) $\{0^n \mid n \text{ in a perfect square}\}$
 ii) The set of strings of 0's and 1's beginning with a 1. Such that when interpreted as an integer, that integer is prime.
 b) Prove the following :
 If L is a regular language, so is L^R .

OR

5. a) If L is language, and a is a symbol, then a/L is the set of strings w such that aw is in L . Prove that if L is regular, so is a/L .
 b) Show that the following grammar G is ambiguous. $S \rightarrow SbS/a$.

(5x10=)
umber

6. Design PDA for the language

$L = \{a^{3n} b^n \mid n \geq 0\}$ and simulate its action on the input string aaaaaabb.

OR

7. a) What is Chomsky normal form ? Convert the given grammar into Chomsky normal form.

- $S \rightarrow ABa$
- $A \rightarrow aab$
- $B \rightarrow Ac$

b) Convert the following grammar to a PDA :

- $S \rightarrow aABB/aAA$
- $A \rightarrow aBB/a$
- $B \rightarrow bBB/A$
- $C \rightarrow a.$

8. What is Turing Machine ? Explain the working of Turing Machine with a neat sketch.

OR

9. Design Turing Machine for the following language :

$L = \{0^n 1^n \mid n \geq 1\}.$

10. Explain in detail :

- i) Multi tape Turing Machine.
- ii) Non-Deterministic Turing Machine.

OR

11. a) Explain the halting problem. Is it decidable or undecidable problem ?

b) Show that the language L and its complement L^c are both recursively enumerable then L is recursive.