Reg. No. : $\qquad$


Name: $\qquad$ .
-
V Semester B.A./B.Sc./B.Com./B.B.A./B.B.A.T.T.M./B.B.M./B.C.A./B.S.W./ B.A. Afsal UI Ulama Degree (CCSS - Reg./Supple./Improv.)

Examination, November 2012 OPEN COURSE IN MATHEMATICS 5D01 MAT : Business Mathematics

Time: 2 Hours
Max. Weightage: 20
Instruction: Answer to all questions.
PART-A

This Part consists of two bunches of questions carrying equal weighage of one. Each bunch consists of four objective type questions. Answer all questions.

Fill in the blanks :

1. $A$ fun $f(x)$ is said to be even if $f(-x)=$
2. $\lim _{x \rightarrow 0} \frac{a^{x}-1}{x}=$ $\qquad$
3. $\frac{d}{d x}(\sqrt{x})=$ $\qquad$
4. $\operatorname{lmt}_{x \rightarrow 0}\left(\frac{x+2}{x-2}\right)=$ $\qquad$
Choose the correct answer for the following :
5. $\frac{d}{d x}\left(e^{m x}\right)=$ $\qquad$
a) $e^{m x}$
b) $m e^{m x}$
c) $m$
d) none of these
6. $\int \frac{1}{1+\mathrm{x}^{2}} \mathrm{dx}=$ $\qquad$
a) $\sin ^{-1}(x)+c$
b) $\cos ^{-1} x+c$
c) $\tan ^{-1}(x)+c$
d) none of these
7. $\int \frac{1}{2} d x=$ $\qquad$
a) $\frac{1}{2}$
b) $x$
c) $\frac{1}{2} x+c$
d) none of these
8. $\lim _{x \rightarrow \infty} \frac{x^{2}+1}{2 x^{2}+4}=$
a) 1
b) 4
c) $1 / 4$
d) $\frac{1}{2}$

Answer any six from the following (Weightage one each).
9. Draw the graph of the function $y=|x|$.
10. Integrate $\log x$ with respect to $x$.
11. Find $\frac{d y}{d x}$ if $y=x^{x}$.
12. Find $\frac{d y}{d x}$ if $y=x^{3} e^{x}$.
13. Differentiate with respect to $x f(x)=\frac{x^{3}+3 x^{2}-4}{x}$.
14. Integrate with respect to $x$; $\sqrt{3 x^{2}-4} .6 x$.
15. Evaluate $\int \frac{x^{5}+8 x^{2}+1}{x^{2}} d x$
16. Find $\lim _{x \rightarrow \infty} \frac{1^{2}+2^{2}+3^{2}+\ldots+x^{2}}{x^{3}}$
17. The demand for a certain product is represented by the equation $p=20+5 q-q^{2}$. Where $q$ is the number of units demanded and $p$ is the price per unit. Find marginal revenue function.
18. Write the condition for a function $y=f(x)$ to have a local minimum at $x$.
PART-C

Answer any four questions. Each carries a weightage of two.
19. Find the points of discontinuity of the function $f(x)=\frac{x^{2}+2 x+5}{x^{2}-3 x+2}$
20. Find the gradient of the curve $y=3 x^{2}-5 x+4$ at the point $(1,2)$.
21. Evaluate $\int \frac{x^{2}}{x+1} d x$
22. Evaluate $\int x e^{x} d x$.
23. The total cost $C(x)$ associated with producing and marketing $x$ units of an item is given by $C(x)=0.005 x^{3}-0.02 x^{2}-30 x+3000$. Find:
i) Total cost when output is 4 units.
ii) Average cost of output of 10 units.
24. Kapil deposited some amount in a bank for $7 \frac{1}{2}$ years at the rate of $6 \%$ per annum (simple interest). Kapil received Rs. 101500 at the end of the term. Compute the initial deposit of Kapil.
25. If $f^{\prime}(x)=8 x+1$ and $f(0)=0$ find $f(z)$.
26. Find $\frac{d y}{d x}$ if $x^{2}-x y+y^{2}=1$.

## PART-D

Answer any one from the following (Weightage four) :
27. Is the function $f(x)=|x|$ continuous at $x=0$.
28. Suppose a manufacture can sell $x$ items per week at a price $P=20-0.001 x$ rupees each when it costs, $y=5 x+2000$ rupees to produce $x$ items. Determine the number of items he should produce per week for maximum profit.
29. Compute the compound interest on Rs. 4,000 for $1 \frac{1}{2}$ years at $10 \%$ per annum compounded half yearly.

